

#41 RECOGNIZING INTEGRALS 7.1

Although the integrals in each group below have similarities, they require different approaches. For each integral decide which of the following is needed: 1) substitution, 2) algebra or a trig identity, 3) nothing needed, or 4) can't be done by the techniques in Calculus I. Then evaluate each integral (except for the 4th type of course).

1. A. $\int (x^3 + 1) dx$

B. $\int x^2 (x^3 + 1)^4 dx$

C. $\int \sqrt{x^3 + 1} dx$

D. $\int (x^3 + 1)^2 dx$

2. A. $\int e^{-x^2} dx$

B. $\int \frac{e^x}{3 + e^x} dx$

C. $\int (e^x + 3) dx$

D. $\int \frac{\ln(e^{2x})}{x^2} dx$

3. A. $\int \sqrt{x} (1 - x^2) dx$

B. $\int \sqrt{1 - x^2} dx$

C. $\int \frac{1}{\sqrt{1 - x^2}} dx$

D. $\int \frac{xdx}{\sqrt{1 - x^2}}$

4. A. $\int \cos\left(\frac{\pi}{4}\right) dx$

B. $\int \sqrt{1 - \cos^2 x} dx$

C. $\int \frac{dx}{\cos x \sqrt{\sin x}}$

D. $\int \frac{\cos x}{\sqrt{\sin x}} dx$

5. A. $\int \tan(3x) \sec(3x) dx$

B. $\int \frac{dx}{\cos^2 x}$

C. $\int \tan x \cos x dx$

D. $\int \frac{dx}{\tan x + 1}$